



Advanced Analytics &
Business Consultancy



GUROBI
OPTIMIZATION

Analytical Revenue Management

Webinar

 April 2023



Agenda

Analytical Revenue Management

Revenue management and fleet rotation at Sixt

Modeling revenue management and fleet rotation

Implementation details

Conclusions



SIXT PORTUGAL

- **Rent-a-car company**, one of the top rent-a-car companies in Europe
- Franchising in **Portugal**, since 2015
- **~40 stations**, organized in pools
- ~10,000 cars, organized in **52 vehicle groups** (Ex. Family, SUV, etc)
- **Pricing** sets the prices and **fleet rotation** distributes the fleet among the stations



[Carros](#) [Carrinhas](#)

Levantamento & devolução

Porto Aeroporto

 Devolver na estação de levantamento

Recolha Data

13. abr

08:00

Data de devolução

14. abr

20:00

[> Aplicar a tarifa empresarial](#)

41 OFERTAS

TIPO DE VEÍCULO ▾

APENAS AUTOMÁTICOS

IDADE DO CONDUTOR 30+ ▾

Nº DE LUGARES 2+ ▾

PREÇO ASCENDENTE ▾

Renault Clio Bi-Fuel

ou similar | Sedan

**Bi-Fuel**

✓ incl. unlimited km

36,26 € | dia
72,51 € total**Renault Clio**

ou similar | Sedan



✓ incl. unlimited km

36,26 € | dia
72,51 € total**Fiat 500**

ou similar | Sedan



✓ incl. unlimited km

36,26 € | dia
72,51 € total**Renault Twingo**

ou similar | Sedan



✓ incl. unlimited km

36,26 € | dia
72,51 € total**Renault Megane Sports Tourer**

ou similar | Station wagon



✓ incl. unlimited km

38,40 € | dia
76,79 € total**Renault Captur**

ou similar | SUV



✓ incl. unlimited km

42,12 € | dia
84,23 € total**Lucky Dip Car**

ou similar | Sedan



✓ incl. unlimited km

42,33 € | dia
84,66 € total**Nissan Qashqai**

ou similar | SUV



✓ incl. unlimited km

49,45 € | dia
98,90 € total

Pain-points



Tactical and operational decisions are **not integrated**



Pricing is defined **empirically**, depending on fleet occupancy rate and competition rates

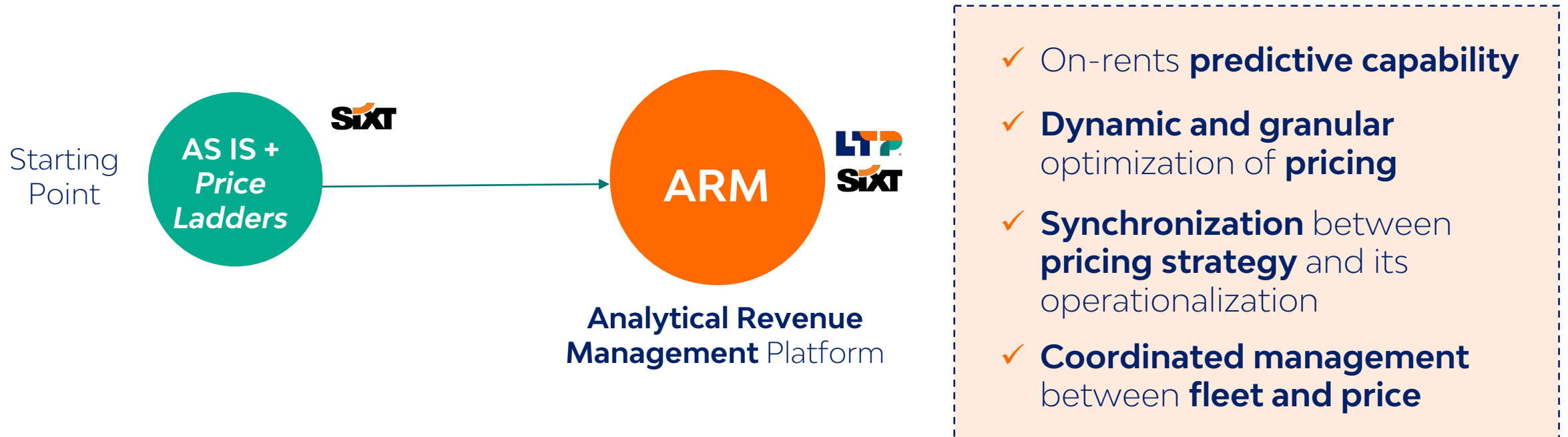


Fleet allocation and pricing are **not integrated**



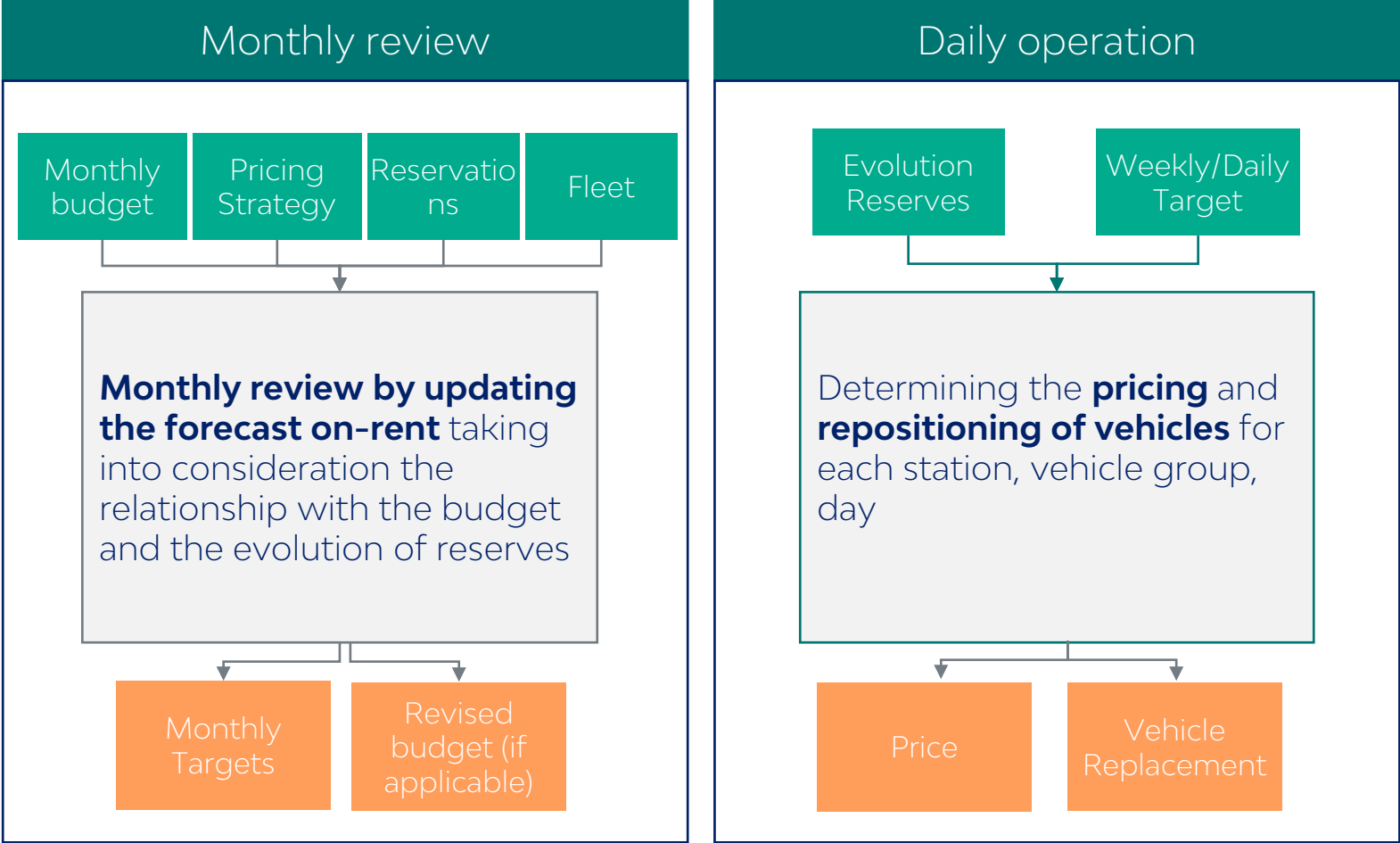
Lack of ability to make pricing and fleet decisions (and operationalize) in **real time**

ARM focused on developing a *revenue management* analytics platform

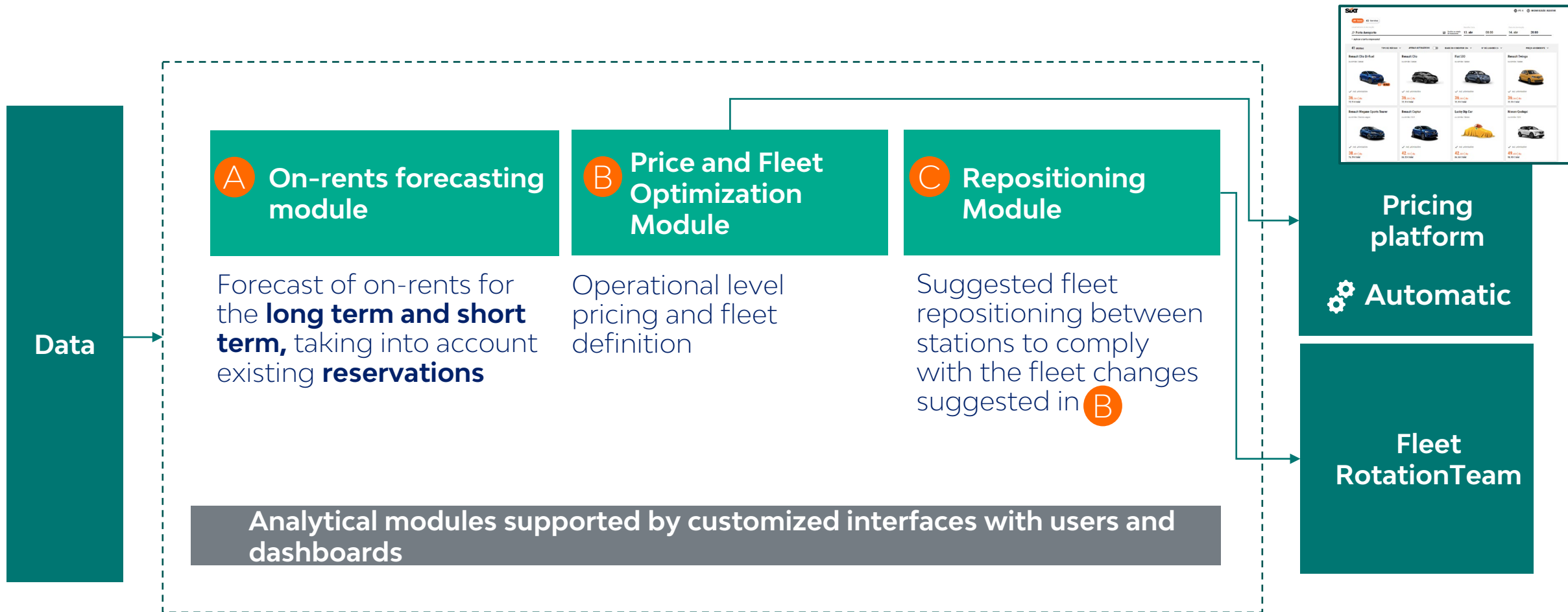


ARM supports both medium- and short-term planning

Inputs Outputs



The revenue management platform has 3 main analytical modules behind the various decisions managed



Details of the methodology explored in the "methodology" section

A The causal predictive model takes into account a broad set of drivers that will impact the forecast generated

Factor Identification

20+ features tested to select the ones that influence on-rents (e.g. historic on-rents, prices, fleet, budget)

Selection and collection of the factors that have a **direct influence on** on-rents

Estimation of the impact of the factors

Advanced Causal Engine (*machine learning*)¹



Reservations in History

Evaluation of the impact of each factor on expected reserves, through an analysis of historical information, and **estimation of expected reserves as a function of the value attributed to each factor**

Generating outputs and gaining insights

On-rents for the one-year horizon



Forecast on-rents for a given date / vehicle group / station



Insights into the influence of different factors on forecasts

Using the Predictive Model to (1) predict on-rents (2) generate insights

¹ Gradient Boosting Machine and Random Forest models

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LTP is a boutique analytical-driven management consultancy



Advanced Analytics &
Business Consultancy

A **proven data-driven approach** enables LTP to address the complex challenges faced by its clients.

LTP combines **advanced analytics with business expertise** to deliver significant and sustainable impact in **bottom line profitability**.



**70+ consultants
+ extended network**



300+ projects



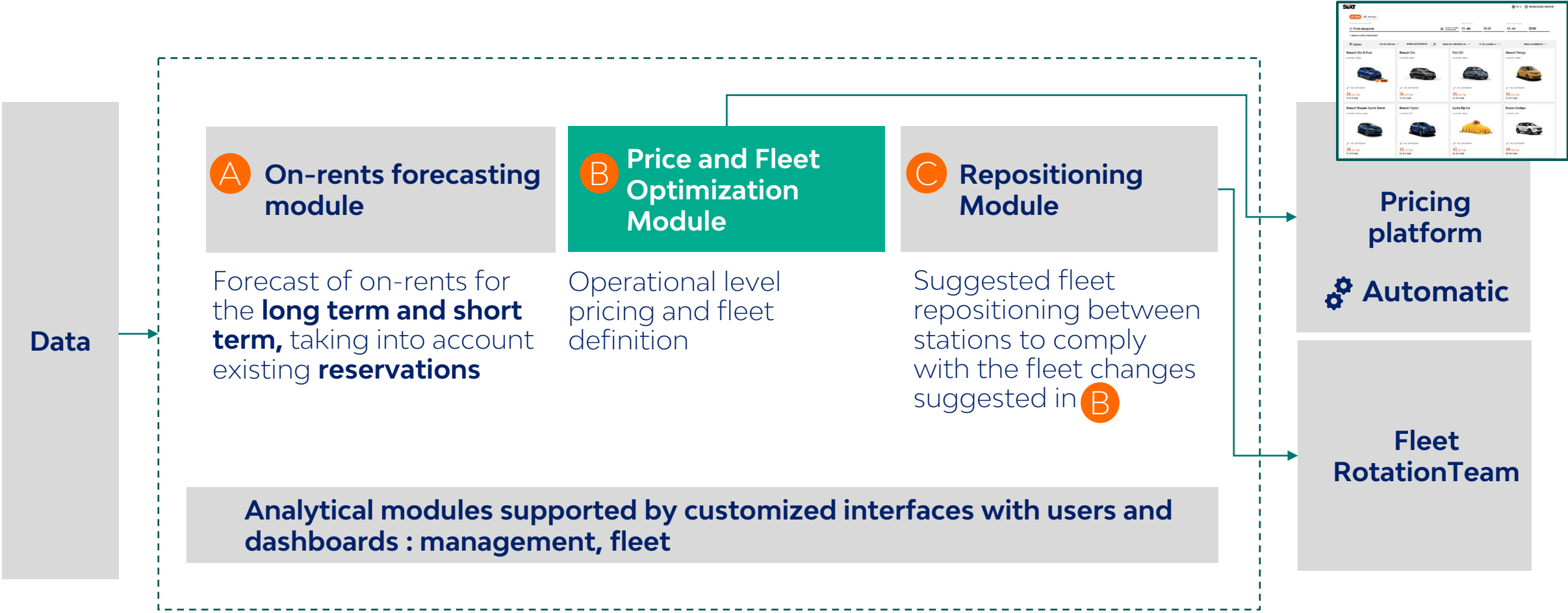
15+ countries



>25% annual growth¹

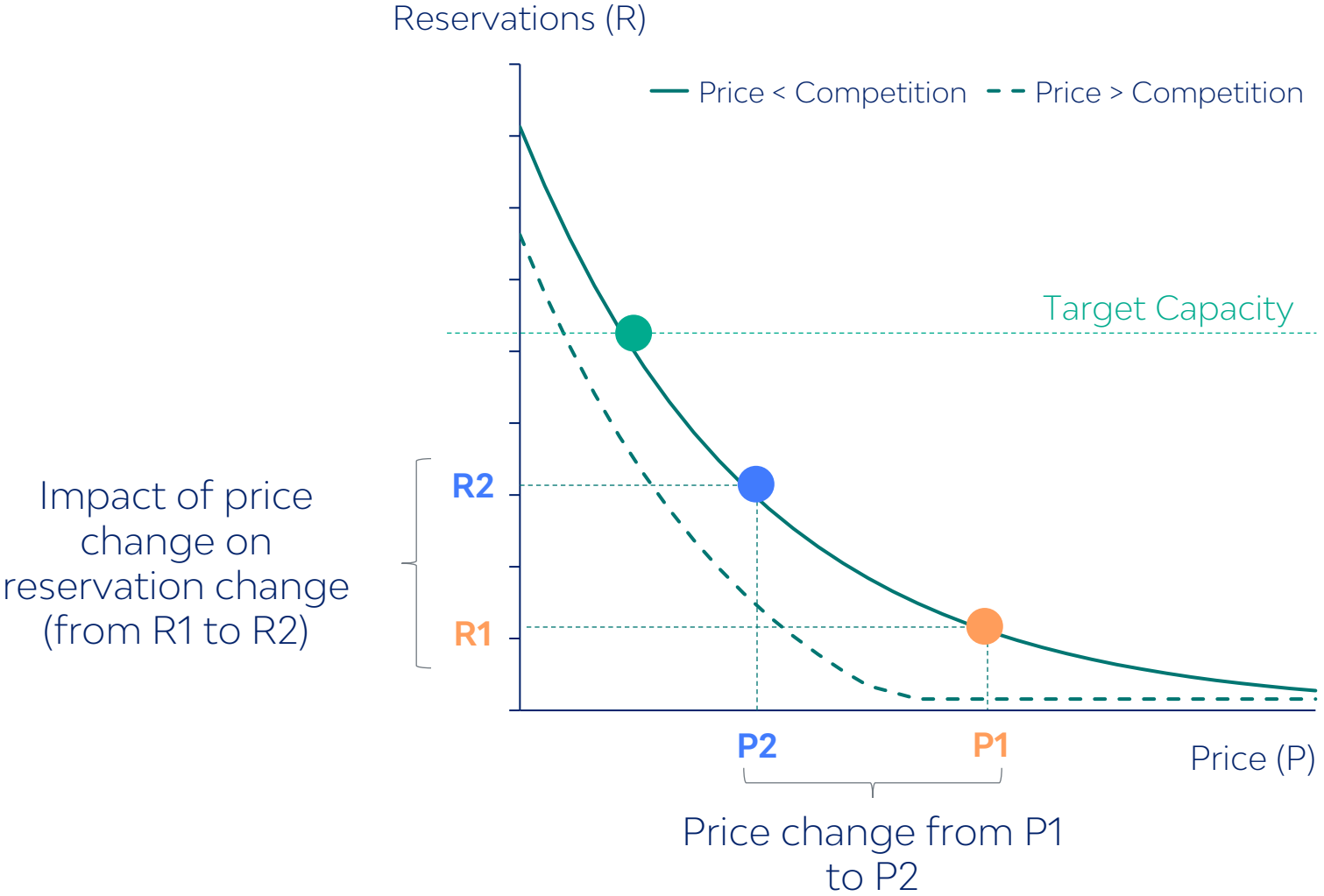
¹ Annual growth rates always above 25% in the past 5 years

The revenue management platform has 3 main analytical modules behind the various decisions managed



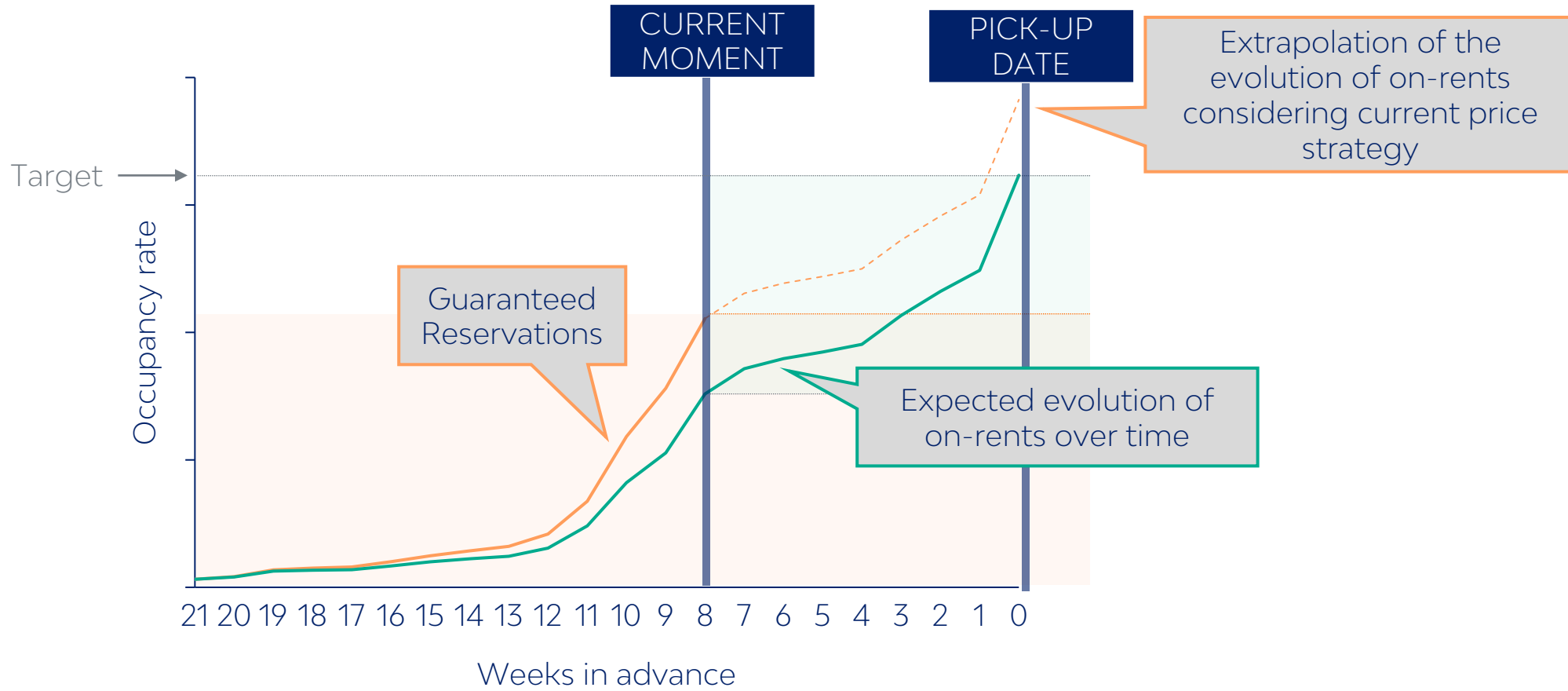
Details of the methodology explored in the "methodology" section

The price elasticity curve allows to assess the extent to which reducing the price leads to a revenue increase



The new approach to pricing and fleet distinguishes itself by its dynamism and target occupancy rate

Evolution of fleet occupancy rate for a given day, along the reservation period

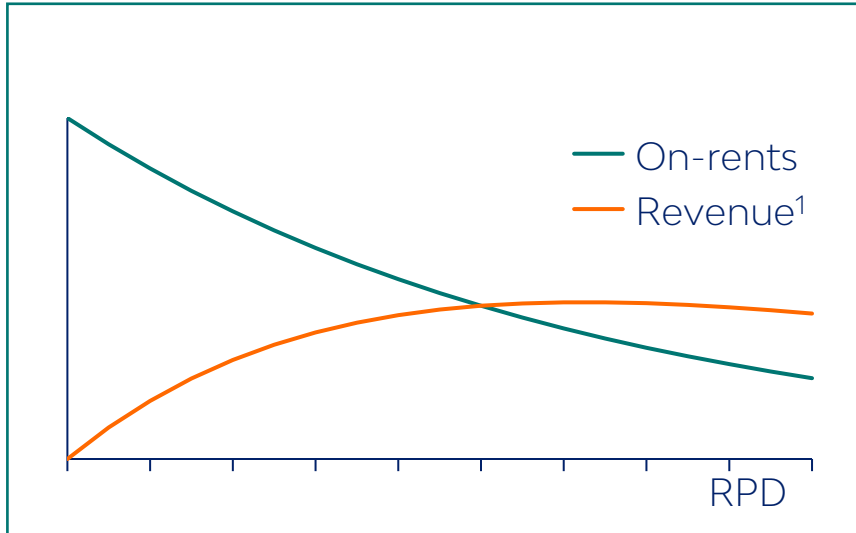


Three main inputs feed the recommendations made, at the station and fleet level

Forecast on-rents

A On-rents forecasting module

Elasticity curves



Parameterizations

Relative to operational constraints and strategic objectives

Station	Fleet	RPD
Station A	+153	19,1€
Station B	+97	15,2€
Station C	+66	15,2€
Station D	-19	15,8€
Station E	-72	16,9€
Station F	-270	15,1€

Weighted average values

The optimization model allows to holistically manage the price while safeguarding constraints between groups and days

Decisions	<ul style="list-style-type: none"> • Price to apply each pickup day, station, group, length of rental • Fleet needed at each station, vehicle group, day
Objective	<ul style="list-style-type: none"> • Revenue/profit maximization
Constraints	<ul style="list-style-type: none"> • Compliance with expected targets (with thresholds for exploitation of goal) • Minimum/maximum price to apply • Relationship between the prices of the vehicle groups • Minimum/maximum fleet at each station • Operational Capacity

Station	Group	Length	Day						
			D1	D2	D3	D4	D5	...	
Station A	Vehicle group 1	Already secured	█	█	█	█	█	█	█
		Length 1, D1	█	█	█	█	█	█	█
		Length 2, D1	█	█	█	█	█	█	█
		... Length 30, D1	█	█	█	█	█	█	█
		Length R 1, D2	█	█	█	█	█	█	█
		Length 2, D2	█	█	█	█	█	█	█
		... Length 30, D2	█	█	█	█	█	█	█
		...							
		Fleet	█	█	█	█	█	█	█
		Station B	Vehicle group 1	Fleet	█	█	█	█	█
		Total Fleet Group 1	█	█	█	█	█	█	

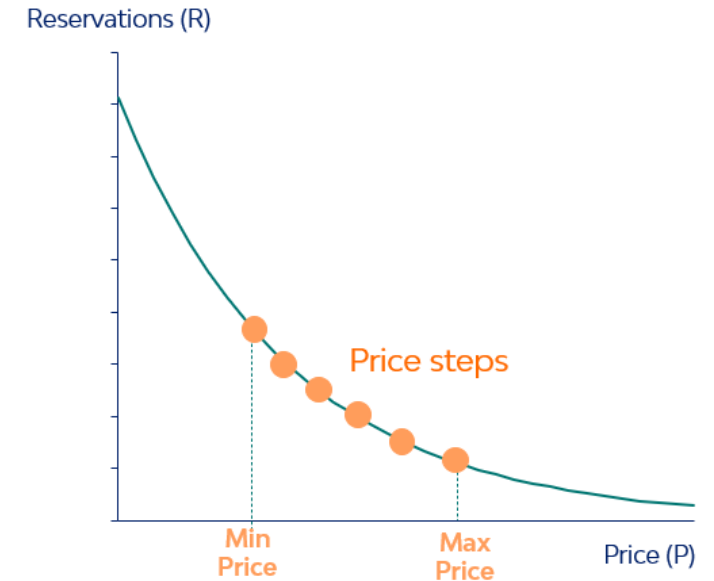
The use of price steps allowed us to linearize the non-linear price-demand relation

Sets and subsets

K	Price Steps
L	LORs
V	Vehicle groups
P	Pools
S	Stations
$S_p \subset S$	Subset of stations that belong to pool p
R	Set of reservation days in the time horizon
U	Set of pick-up days in the time horizon

Decision variables

d_{vsluk}	Price step k selected for vehicle group v in station s , with LOR l , on pick-up day u . Each price step has a given revenue per day price. If price step k is selected, then $d_{vsluk} = 1$. If not, $d_{vsluk} = 0$.
f_{vsr}	Fleet level for vehicle group v in station s , on reservation day r . This decision variable will be an input for the vehicle repositioning model. This decision variable defines the target fleet of vehicle group v to have in station s on reservation day r .
w_{vpr}	Fleet decrease for vehicle group v in pool p , on reservation day r . This variable represents the number of vehicles v that the car rental company should remove from pool p .
x_{vpr}	Fleet increase for vehicle group v in pool p , on reservation day r . The variable represents the number of vehicles v that the car rental company should bring to pool p .
y_{vsr}	Fleet decrease for vehicle group v in station s , on reservation day r . This variable represents the number of vehicles v that the car rental company should remove from station s .
z_{vsr}	Fleet increase for vehicle group v in station s , on reservation day r . The variable represents the number of vehicles v that the car rental company should bring to station s .



The objective function maximizes overall profit by considering the revenue generated by future reservations minus costs

Objective function

$$\begin{aligned}
 \max \sum_{v \in V} \sum_{s \in S} \sum_{r \in R} & \left[\sum_{l \in L} \sum_{u \in U} \sum_{k \in K} (d_{vsluk} \times RP_{vsluk} \times (RPD_{vsluk} - CPD_{vsluk}) \times \alpha_{rlu}) \times (1 - OR_{vsr}) \right] \quad 1 \text{ Expected future profit} \\
 & - \sum_{v \in V} \sum_{s \in S} \sum_{r \in R} ((M_1 \times \delta_r + CS_s) \times z_{vsr}) \\
 & - \sum_{v \in V} \sum_{p \in P} \sum_{r \in R} ((M_1 \times \rho_r + CP_p) \times x_{vpr}) \quad 2 \text{ Overall fleet repositioning costs between stations and pools} \\
 & \quad (4.1)
 \end{aligned}$$

The model contains 7 major groups of constraints mostly related with fleet constraints, target on-rents and price orders

Constraints (1/3)

$$\sum_{k \in K} d_{vsluk} = 1 \quad \forall v \in V, s \in S, l \in L, u \in U \quad (4.2)$$

$$AF_{vrs} - AF_{v,s,r-1} + f_{v,s,r-1} + z_{vrs} - y_{vrs} = f_{vrs} \quad \forall v \in V, s \in S, r \in R \quad (4.3)$$

$$\sum_{s \in S_p} (AF_{vrs} - AF_{v,s,r-1}) + f_{v,p,r-1} + x_{vpr} - w_{vpr} = \sum_{s \in S_p} f_{vrs} \quad \forall v \in V, p \in P, r \in R \quad (4.4)$$

$$\sum_{s \in S} AF_{vrs} = \sum_{s \in S} f_{vrs} \quad \forall v \in V, r \in R : \delta_r = 1 \quad (4.5)$$

$$FS_s \leq \sum_{v \in V} f_{vrs} \quad \forall s \in S, r \in R : \delta_r = 1 \quad (4.6)$$

$$FP_p \leq \sum_{v \in V} \sum_{s \in S_p} f_{vrs} \quad \forall p \in P, r \in R : \delta_r \times \rho_r = 1 \quad (4.7)$$

1

Only one **price step**

2

Fleet constraints:

- Fleet size at each station depends on previous transfers and existing vehicles
- Total fleet size
- Minimum station fleet and pool fleet

The model contains 7 major groups of constraints mostly related with fleet constraints, target on-rents and price orders

Constraints (2/3)

$$\sum_{l \in L} \sum_{k \in K} \sum_{u \in U} (d_{vsluk} \times RP_{vsluk} \times \alpha_{rlu}) \times (1 - OR_{vsr}) + \sum_{l \in L} \sum_{u \in U} (RC_{vslu} \times \alpha_{rlu}) \geq f_{vsr} \times OG_{vsr}^- \quad \forall v \in V, s \in S, r \in R \quad (4.8)$$

$$\sum_{l \in L} \sum_{k \in K} \sum_{u \in U} (d_{vsluk} \times RP_{vsluk} \times \alpha_{rlu}) \times (1 - OR_{vsr}) + \sum_{l \in L} \sum_{u \in U} (RC_{vslu} \times \alpha_{rlu}) \leq f_{vsr} \times OG_{vsr}^+ \quad \forall v \in V, s \in S, r \in R \quad (4.9)$$

$$\sum_{v \in V} \left[\sum_{l \in L} \sum_{k \in K} \sum_{u \in U} (d_{vsluk} \times RP_{vsluk} \times \alpha_{rlu}) \times (1 - OR_{vsr}) \right] + \sum_{v \in V} \sum_{l \in L} \sum_{u \in U} (RC_{vslu} \times \alpha_{rlu}) + SF_s \geq \sum_{v \in V} f_{vsr} \quad \forall s \in S, r \in R \quad (4.10)$$

$$\sum_{v \in V} \sum_{s \in S_p} \left[\sum_{l \in L} \sum_{k \in K} \sum_{u \in U} (d_{vsluk} \times RP_{vsluk} \times \alpha_{rlu}) \times (1 - OR_{vsr}) \right] + \sum_{v \in V} \sum_{s \in S_p} \sum_{l \in L} \sum_{u \in U} (RC_{vslu} \times \alpha_{rlu}) + PF_p \geq \sum_{v \in V} \sum_{s \in S_p} f_{vsr} \quad \forall p \in P, r \in R \quad (4.11)$$

$$\sum_{v \in V} \sum_{s \in S} z_{vsr} \leq TD \quad \forall r \in R \quad (4.12)$$

$$\sum_{v \in V} \sum_{s \in S_p} z_{vsr} \leq PD \quad \forall p \in P, r \in R \quad (4.13)$$

3

Total **on-rents per day** between minimum and maximum target occupancy **target**

4

Maximum fleet parked at the same time at each station

5

Maximum transfers between stations and pool

Total on-rents per day

Station	Group	Length	Day						
			D1	D2	D3	D4	D5	...	
Station A	Vehicle group 1	Already secured	█	█	█	█	█	█	█
		Length 1, D1	█	█	█	█	█	█	█
		Length 2, D1	█	█	█	█	█	█	█
		... Length 30, D1	█	█	█	█	█	█	█
		Length R 1, D2	█	█	█	█	█	█	█
		Length 2, D2	█	█	█	█	█	█	█
		... Length 30, D2	█	█	█	█	█	█	█
		...							
	Fleet	█	█	█	█	█	█	█	
Station B	Vehicle group 1	Fleet	█	█	█	█	█	█	█
	Total Fleet Group 1	█	█	█	█	█	█	█	

The model contains 7 major groups of constraints mostly related with fleet constraints, target on-rents and price orders

Constraints (3/3)

$$\sum_{v \in V} \left[\sum_{l \in L} \sum_{k \in K} (RP_{vsluk} \times d_{vsluk}) \times (1 - OP_{vsu}) \right] +$$

$$\sum_{v \in V} RC_{vslu} \leq OC_s \quad \forall s \in S, u \in U \quad (4.14)$$

6 Daily **operational capacity**

$$\sum_{k \in K} d_{vLsluk} \times RPD_{vLsluk} \leq$$

$$\sum_{k \in K} d_{vsluk} \times RPD_{vsluk} \quad \forall v \in V, v_L = VL_{vslu},$$

$$s \in S, l \in L, u \in U \quad (4.15)$$

7 **Price order** between vehicle groups

$$\sum_{k \in K} d_{vsluk} \times RPD_{vsluk} \leq$$

$$\sum_{k \in K} d_{vHsluk} \times RPD_{vHsluk} \quad \forall v \in V, v_H = VH_{vslu},$$

$$s \in S, l \in L, u \in U \quad (4.16)$$

$$d_{vsluk} \in (0, 1) \quad \forall v \in V, s \in S, l \in L, u \in U, k \in K \quad (4.17)$$

$$f_{vsr} \in \mathbb{R}_0^+ \quad \forall v \in V, s \in S, r \in R \quad (4.18)$$

$$w_{vpr} \in \mathbb{R}_0^+ \quad \forall v \in V, p \in P, r \in R \quad (4.19)$$

$$y_{vsr} \in \mathbb{R}_0^+ \quad \forall v \in V, s \in S, r \in R \quad (4.20)$$

$$x_{vpr} \in \mathbb{R}_0^+ \quad \forall v \in V, p \in P, r \in R \quad (4.21)$$

$$z_{vsr} \in \mathbb{R}_0^+ \quad \forall v \in V, s \in S, r \in R \quad (4.22)$$

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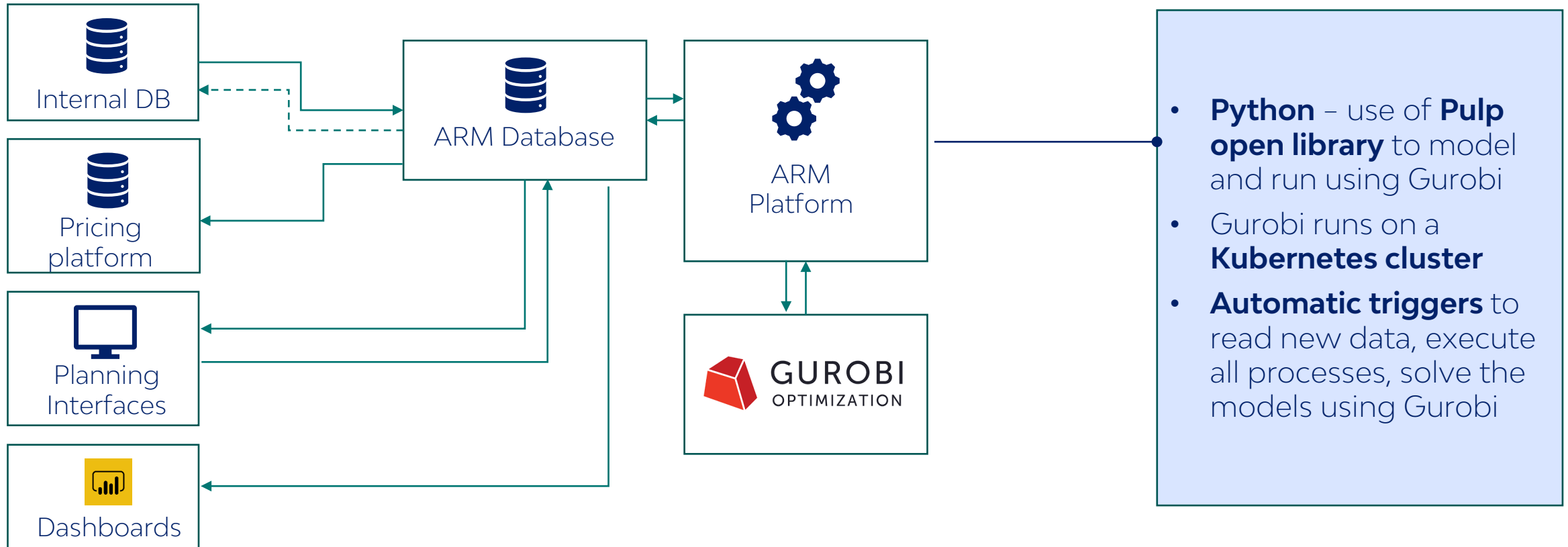
Modeling revenue management and fleet rotation

Implementation details

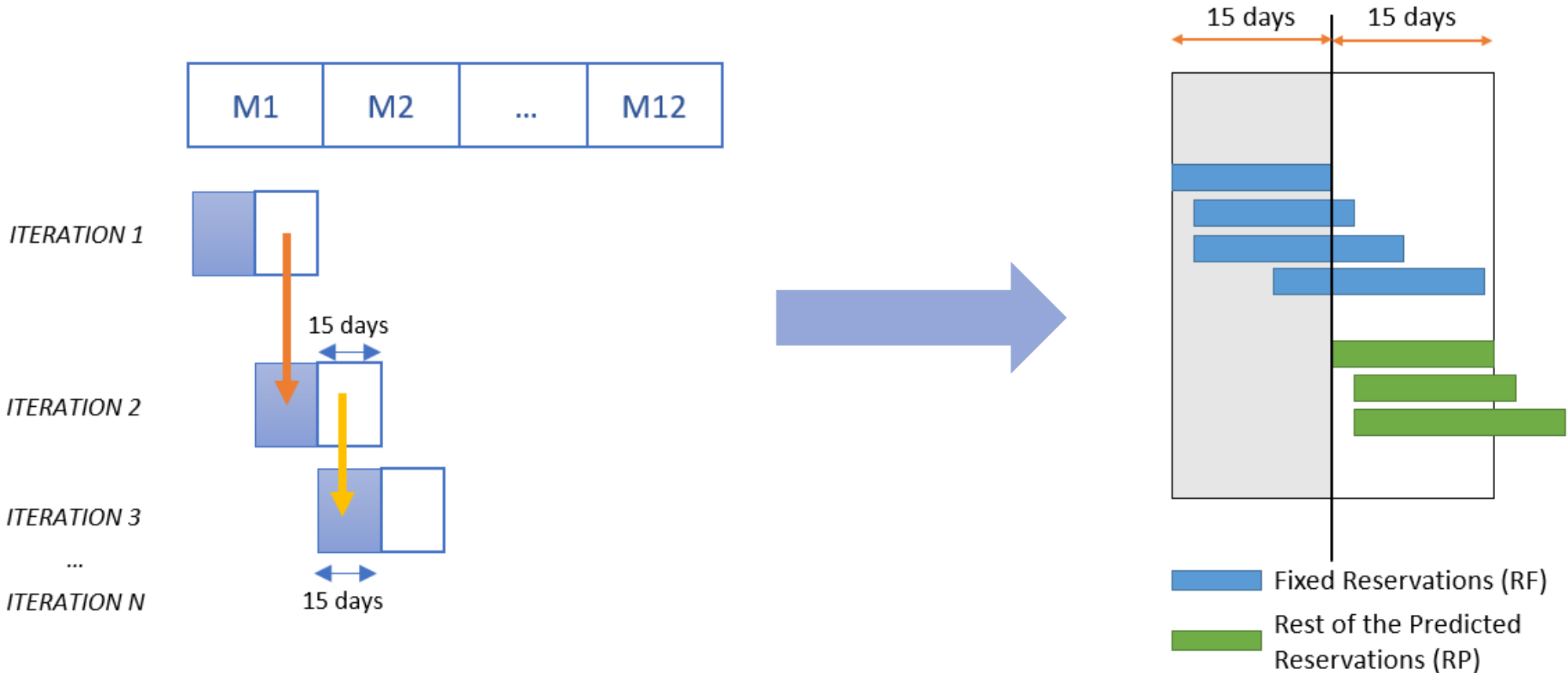
Conclusions



The ARM platform is integrated with Sixt's servers



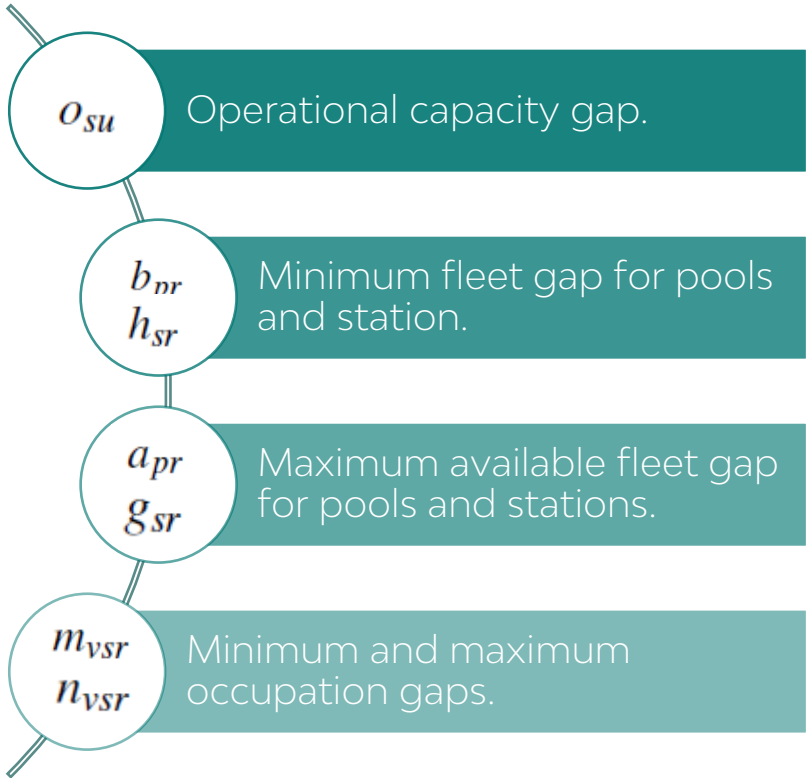
A relax-and-fix method was implemented to tackle the model complexity challenge



A solution approach was developed to tackle the challenges in the implementation of the model

Data Issues

Add gaps to the model.



Time Execution Challenge

BigM	Reevaluate the BigM of the objective function
Parameters	Finetune the parameters
Decision Variable	Transform all decision variables in continuous
Server	Improve server's specifications
Planning Horizon	Reduce the number of months to output new values daily

↓ **x9** Faster

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Conclusions

- More information, with greater granularity that allow Sixt to make **more, better and faster decisions** – potential to generate **1.5 million of prices per day**
- **Greater control**, provided by the tactical integration and the alarmistic system that ensure the necessary validation of extreme cases
- **Faster and semi-automatic reaction** to price/occupancy rate variations
- Preliminary projections point to a **2% to 8% revenue increase**
- **Change of paradigm** with high impact on the team



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WITH ANALYTICS

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